# Collusion between Supply Chains under Asymmetric Information\*

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#### Abstract

This paper considers an infinitely repeated competition between manufacturer-retailer supply chains. In every period, retailers privately observe the demand and manufacturers pay retailers "information rents". I study collusive equilibria between the supply chains that may or may not involve the retailers. I find that including forward-looking retailers in the collusive scheme may facilitate or hinder collusion, depending on the likelihood of a high demand and the gap between a high and a low demand. Moreover, collusion on monopoly profits can be easier or more difficult to implement than collusion on upstream profits.

**Keywords:** vertical relations, collusion, asymmetric information

JEL Classification Numbers: L22, L42, D82

### 1 Introduction

Competition between vertical manufacturer-retailer supply chains may involve both repeated interaction between the supply chains and long-term relationship within each supply chain. Manufacturers typically engage in an on-going competition with other manufacturers. Such repeated interaction enables manufacturers to horizontally collude on restricting competition.

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At the same time, manufactures may also engage in long-term relationships with their retailers and may use the retailers' help to facilitate collusion.

The possibility of collusion in a market with repeat interaction between supply chains and within each supply chain raises two main questions. First, are retailers helpful or harmful to such collusion? Manufacturers may exclude retailers from the collusive scheme by dealing with myopic retailers, switching between retailers in each period, or by ignoring retailers' deviations from collusion. Alternatively, manufacturers may include forward-looking retailers in the collusive scheme, such that collusion breaks following a retailer's deviation. In such a case, collusion is also "vertical" because it includes the retailers. This raises the question of whether retailers facilitate or hinder collusion. The second question is whether collusion on the monopoly outcome is easier to maintain than collusion on maximizing upstream profits. Because manufacturers share some of the collusive profits with the retailers, manufacturers prefer to collude on maximizing upstream profits rather than the total monopoly profits. This raises the question of what are the features of the collusive outcomes on upstream profits. Moreover, whether collusion on upstream profits is easier to maintain than collusion on the monopoly profits.

The answers to these questions can explain why in recent years, some collusion cases involved the active participation of the retailers, such that retailers were part of the collusive scheme and were able to break collusion. Yet, other collusion cases involved retailers' passive adherence to the manufacturers' collusion, or even attempts to break the collusive scheme. For example, in 2021, the Germany's Federal Cartel Office (FCO) fined leading music instruments manufacturers and their retailers for limiting price competition. According to the FCO: "For years, manufacturers and retailers of musical instruments have systematically endeavoured to restrict price competition for the end consumer,..." Accordingly, manufacturers asked retailers "...not to undercut fixed minimum sales prices, which they did in many cases." The collusive scheme involved the active collaboration of retailers, who where closely monitored by their suppliers. This implies that a retailer's deviation from collusion could break the collusive scheme, though retailers chose to support and facilitate collusion. As an opposite example, a federal appeals court in San Francisco ruled in 2022 against two leading canned tuna manufacturer for alleged collusive scheme to inflate prices to restaurants and retailers. In this case, retailers were not part of the collusive scheme and in fact attempted

<sup>&</sup>lt;sup>1</sup>See Bundeskartellamt, 2021.

to stop it by suing their suppliers.<sup>2</sup>

This paper considers an infinitely repeated competition between two manufacturer-retailer supply chains. At the beginning of each period, retailers privately observe the demand, which is i.i.d between periods. Each manufacturer offers its retailer a menu of contracts valid for this particular period and each retailer chooses a contract from the menu. Manufacturers design a menu that solicits retailers to reveal their private information by their contract selections. To so so, manufactures need to share some of their collusive profits with their retailers, in the form of "information rents". At the end of the period, all information becomes common knowledge. In particular, each manufacturer observes the demand realization as well as the menu offer of the competing supply chain and quantities.

I study collusive equilibria in which the two manufacturers offer the same collusive menu in all periods and retailers choose the contract from the menu that corresponds to the true state of demand. An observable deviation from the collusive equilibrium triggers the competitive, static equilibrium in all future periods. In the context of this model, collusive equilibria can vary in two dimensions. The first dimension is whether retailers are included or excluded from the collusive scheme. In the former case, the collusive equilibrium breaks once a retailer deviates by choosing a contract that corresponds to the wrong state of demand or by rejecting the menu all together. In the latter case, manufacturers ignore a retailer's deviation from the collusive path and continue to collude. The second dimension concerns the profit that firms collude on. Firms may collude on maximizing monopoly profits: the joint profit of the four firms. Alternatively, firms may collude on maximizing the joint upstream profits only.

The paper establishes the following results. First, retailers hinder collusion when the probability of a high demand is low, and may facilitate collusion otherwise. In the latter case, the lowest discount factor that enables firms to collude when retailers take part of the collusive scheme is lower than the equivalent discount factor when retailers are myopic or when manufacturers ignore retailers' deviations. The intuition for this result is that when the retailers' expected information rents given the collusive quantities are higher than given the static outcome, including retailers in the collusive scheme motivates them to truthfully reveal their private information. This is because retailers expect that should they miss-represent the state of demand in a certain period, collusion stops in all future periods as retailers take part in the collusive scheme. This enables manufacturers to reduce the information rents,

<sup>&</sup>lt;sup>2</sup>See Competition Policy International, 2022.

in comparison with the case in which a retailer's deviation does not stop collusion, and to facilitate collusion. In contrast, when retailers' expected information rents in the static case are higher than under collusion, retailers have an incentive to stop collusion, in which case collusion is easier to maintain when retailers are excluded.

The second main result is that when manufacturers collude on the outcome that maximizes their upstream profits, collusion involves a quantity above (below) the monopoly quantity in high (low) demand. The intuition for this result is that increasing the gap between the quantities in high and low demand reduces the retailers' incentive to miss-represent a high demand as low, which in turn reduces their information rents. Hence, manufacturers collude on reducing each other's retailer's information rents.

The third main result is that collusion on the monopoly quantities is easier to maintain than collusion on upstream profits when the probability of high demand and the gap between the demand in the two states is sufficiently small. Intuitively, manufacturers gain higher profits when colluding on upstream profits than when colluding on monopoly profits. Yet, manufacturers' short-run benefit from defecting from collusion may also be higher when colluding on upstream profits. This is because upstream collusion involves a lower quantity than the monopoly quantity when demand is low and a higher quantity otherwise. Hence, when low demand is more likely, each manufacturer has a stronger incentive to defect from the low quantity by rising its own quantity, although doing so breaks collusion.

To the best of my knowledge, this is the first paper that shows how asymmetric information between a manufacturer and its retailer affects collusion, in a market when retailers can be include or excluded from the collusive scheme. The paper relates to three fields of economic literature. First, it is related to Gal-Or (1991a) and (1991b), Caillaud, Jullien and Picard (1995), Martimort (1996), Yehezkel (2008), Acconcia, Martina and Piccolo (2008) and Yehezkel (2014) that consider static vertical relations with asymmetric information. My paper contributes to this literature by showing how dynamic considerations can solve problems of asymmetric information between manufacturers and retailers, when retailers take part in the collusive scheme.<sup>3</sup>

Second, this paper is related to the literature on dynamic vertical relations. Asker and Bar-Isaac (2014) consider an incumbent supplier that can exclude the entry of a forward-

<sup>&</sup>lt;sup>3</sup>Athey and Bagwell ((2001) and (2008)) consider asymmetric information between horizontal competitors, in the context of horizontal collusion in an infinitely repeated game. I contribute to these papers by considering the role of privately informed retailers in facilitating collusion.

looking entrant by offering forward-looking retailers a share of the incumbent's monopoly profits. Normann (2009) and Nocke and White (2010) studies how vertical integration facilitates downstream collusion between a vertically integrated retailer and independent retailers. Piccolo and Miklós-Thal (2012) consider collusion between competing retailers that offer myopic suppliers a high wholesale price and negative fixed fees. Gilo and Yehezkel (2020) show how retailers can use a forward looking supplier for maintaining collusion, when retailers are too shortsighted to collude by themselves. There are also literature that consider collusion between suppliers, when retailers are myopic. Jullien and Rey (2007) consider a closely related paper to this proposed research, with two competing vertical supply chains facing demand uncertainty. This proposed research focuses instead on asymmetric information concerning the demand. Nocke and White (2007) studies how vertical integration affects upstream collusion. Reisinger and Thomes (2017) compares upstream collusion with a joint and a separate retailer. Piccolo and Reisinger (2011) show how exclusive territories agreements can facilitate upstream collusion. Gilo and Yehezkel (2021) studies collusion between a manufacturer and a retailer on excluding a new product that is initially inferior but can improve is sold over time. All the above papers assume that there is full-information concerning the demand. The main contribution of this paper is by introducing asymmetric information to dynamic vertical relations and by showing how retailers' information rents affect the dynamic equilibria and collusion.

The third strand of related literature concerns with relational-contracts. This literature considers a repeated game between a principal and an agent when the agent has some private information and in addition, the agent can choose an uncontractible, though publicly observable action. In the context of this paper, the relationship between each manufacturer and its retailer can be interpreted as such relational contract. Notable contributions are Levin (2003), Halac (2012), Akifumi (2016) Calzolari and Spagnolo (2017) and Martimort, Semenov and Stole (2017). This paper extends this literature to the case where the agents' private information becomes public at the end of each period, and when there are two competing principal-agent supply chains. In a closely related paper, Shamir and Yehezkel (forthcoming) consider a dynamic relational contract between a monopolistic manufacturer and a monopolistic retailer when the retailer has private information concerning the demand. The focus of this paper is different. Shamir and Yehezkel (forthcoming) focus on the question of whether the retailer would like to share information concerning the demand with the manufacturer

ex-post. This paper assumes that all information becomes public at the end of each period, and focuses on competition and collusion.

### 2 The model and static benchmark

Consider two supply chains,  $M_1 - R_1$  and  $M_2 - R_2$ , where  $M_i$  is an upstream manufacturer that serves the downstream retailer  $R_i$ . The four firms interact for an infinite number of periods and discount future profits by  $\delta$  ( $0 \le \delta \le 1$ ).

In every period, there are two states of demand, high (H) and low (L), with probabilities p and 1-p, respectively. The demand realization is i.i.d between periods. Joint profit of  $M_i - R_i$  (i = 1, 2) in state  $\theta = \{H, L\}$  is  $\pi_{\theta i}(q_i, q_j)$ , where  $q_i$  is the quantity sold by  $R_i$  and  $\pi_{\theta i}(q_i, q_j)$  is an inverse U-shape function of  $q_i$  and decreasing with  $q_j$ . Suppose that  $\pi_{Hi}(q_i, q_j) > \pi_{Li}(q_i, q_j)$  and  $\pi_{Hi}(q_i, q_j) - \pi_{Li}(q_i, q_j)$  is increasing in  $q_i$ . Let  $\partial \pi_{\theta i}(q_i, q_j)/\partial q_i$   $(\partial \pi_{\theta i}(q_i, q_j)/\partial q_j)$  denote the partial derivative of  $\pi_{\theta i}(q_i, q_j)$  with respect to the first (second) argument of  $\pi_{\theta i}(q_i, q_j)$ , respectively, where  $\partial \pi_{\theta i}(q_i, q_j)/\partial q_j < 0$ . The two supply chains may sell horizontally differentiated products, or homogeneous products. The main results are derived given any profit functions satisfying the above assumptions. For results that depend on the model's parameters (in particular, on the gap between  $\pi_{Hi}(q_i, q_j)$  and  $\pi_{Li}(q_i, q_j)$ ), I adopt for simplicity a linear demand function with homogeneous products.

The timing and information structure of each period is the following. At the beginning of the period, the two retailers privately observe whether the demand is H or L in the current period (recall that states are i.i.d.). Each  $M_i$  offers  $R_i$  a take-it-or-leave-it menu  $\{(q_{Hi}, T_{Hi}), (q_{Li}, T_{Li})\}$  from which  $R_i$  chooses a contract, where  $T_{\theta i}$  is a fixed payment for the quantity  $q_{\theta i}$ . If  $R_i$  rejects the menu, there is no trade between  $M_i$  and  $R_i$  in the current period and  $R_j$  is a monopolist. Otherwise,  $R_i$  chooses a contract from the menu. The bilateral contracting stage between  $M_i$  and  $R_i$  is secret:  $R_j$  cannot observe the menu that  $M_i$  offers  $R_i$  and which contract  $R_i$  chooses from the menu, if any. Then, the two retailers sell their receptive quantities.<sup>4</sup> Each  $R_i$  earns  $\pi_{\theta i}(q_{\theta i}, q_{\theta j}) - T_{\theta i}$  and  $M_i$  earns  $T_{\theta i}$ . At the end of the period, all information becomes public, including the contract offers, which contract was chosen and the demand realization.<sup>5</sup>

<sup>&</sup>lt;sup>4</sup>As long as retailers have to sell their entire quantities, the results do not depend on whether retailers compete in prices or quantities.

<sup>&</sup>lt;sup>5</sup>In Shamir and Yehezkel (forthcoming), we study why a retailer may profit from sharing ex-post in-

Let  $q_{\theta}^{C}$  denote the symmetric full-information competitive quantities that correspond to each state  $\theta$ , given that the two supply chains play a static game. The quantities  $q_{\theta}^{C}$  are the solution to:  $\partial \pi_{\theta i}(q_{\theta}^{C}, q_{\theta}^{C})/\partial q_{\theta i} = 0$ . The monopoly quantities that maximize total profits of the two supply chains are  $q_{\theta}^{M}$ , defined by:  $\partial \pi_{\theta i}(q_{\theta}^{M}, q_{\theta}^{M})/\partial q_{\theta i} + \partial \pi_{\theta j}(q_{\theta}^{M}, q_{\theta}^{M})/\partial q_{\theta i} = 0$  (notice that  $q_{\theta}^{M}$  is the quantity that each of the two supply chains should set in order to maximize total industry profits). Because  $\partial \pi_{\theta j}(q_{i}, q_{j})/\partial q_{i} < 0$ , it follows that  $q_{\theta}^{C} > q_{\theta}^{M}$ .

As a benchmark, consider asymmetric information in a static game: firms interact for one period. This benchmark case is also an equilibrium in the dynamic game when firms do not believe that their strategies in the current period affect the equilibrium in future periods. This scenario serves as a useful benchmark because I will assume that a deviation from collusion result in playing the competitive static game indefinitely. Under asymmetric information, each  $M_i$  offers a menu as to maximize the expected profit,  $pT_{Hi} + (1-p)T_{Li}$ , subject to:

$$IR_L^S$$
:  $\pi_{Li}(q_{Li}, q_{Lj}) - T_{Li} \ge 0,$  (1)

$$IC_H^S$$
:  $\pi_{Hi}(q_{Hi}, q_{Hj}) - T_{Hi} \ge \pi_{Hi}(q_{Li}, q_{Hj}) - T_{Li}$ . (2)

Given that  $M_j$  offered  $R_j$  a menu  $\{(q_{Hj}, T_{Hj}), (q_{Lj}, T_{Lj})\}$  and that  $R_j$  accepted a contract that corresponds to the true state,  $M_i$  offers a menu  $\{(q_{Hi}, T_{Hi}), (q_{Li}, T_{Li})\}$  such that  $R_i$  agrees to accept the contract  $(q_{Li}, T_{Li})$  in state L (the static Individual Rationality constraint in state L:  $IR_L^S$ ), and prefers  $(q_{Hi}, T_{Hi})$  over  $(q_{Li}, T_{Li})$  in state H (the static Incentive Compatibility constraint in state H:  $IC_H^S$ ). Solving  $IR_L^S$  and  $IC_H^S$  in equality for  $T_{Hi}$  and  $T_{Li}$  and substituting into  $pT_{Hi} + (1-p)T_{Li}$ , each  $M_i$  earns an expected profit:

$$\Pi_{Mi}^{S}(q_{Hi}, q_{Li}, q_{Hj}, q_{Lj}) = p\pi_{Hi}(q_{Hi}, q_{Hj}) + (1 - p)\pi_{Li}(q_{Li}, q_{Lj})$$
(3)

$$-p\big[\pi_{Hi}(q_{Li},q_{Hj})-\pi_{Li}(q_{Li},q_{Lj})\big].$$

The first two terms are the expected  $M_i - R_i$  joint profit. The term in the squared brackets is the "information rents" that each  $M_i$  needs to leave  $R_i$  in state H, for motivating  $R_i$  to reveal the type by choosing  $(q_{Hi}, T_{Hi})$  instead of  $(q_{Li}, T_{Li})$ . By the assumption that  $\pi_{Hi}(q_i, q_j)$  —

formation with the manufacturer by providing past-sales information. In this paper, the main focus is on competition or collusion between vertical supply chains and hence I make the simplifying assumption that valuable information becomes observable at the end of the period.

<sup>&</sup>lt;sup>6</sup>It is possible to show that  $R_i$ 's participation constraint in state H and incentive compatibility constraint in state L are not binding.

 $\pi_{Li}(q_i, q_j)$  is increasing in  $q_i$ , the information rents,  $\pi_{Hi}(q_{Li}, q_{Hj}) - \pi_{Li}(q_{Li}, q_{Lj})$ , are increasing with  $q_{Li}$  as long as the gap between  $q_{Hj}$  and  $q_{Lj}$  is not too high. Maximizing (3) with respect to  $q_{Hi}$  and  $q_{Li}$  yields the first-order conditions (respectively):

$$\frac{\partial \pi_{Hi}(q_{Hi}, q_{Hj})}{\partial q_i} = 0, \quad \frac{\partial \pi_{Li}(q_{Li}, q_{Lj})}{\partial q_i} - p \frac{\partial \pi_{Hi}(q_{Li}, q_{Hj})}{\partial q_i} = 0.$$
 (4)

Let  $q_{Hi}^S(q_{Hj})$  and  $q_{Li}^S(q_{Lj}, q_{Hj})$  denote  $M_i$ 's best response functions in the static, asymmetric information case (the solution to (4)). Notice that  $q_{Li}^S(q_{Lj}, q_{Hj})$  is a function of both  $q_{Lj}$  and  $q_{Hj}$ . The symmetric equilibrium quantities in the static game with asymmetric information,  $q_L^S$  and  $q_H^S$ , are the solutions to:  $q_H^S = q_H^S(q_H^S)$  and  $q_L^S = q_L^S(q_L^S, q_H^S)$ . It is straightforward to see that  $q_H^S = q_H^C$  and  $q_L^S < q_L^C$ . I assume that p is not too high to induce  $q_L^S = 0.7$ 

As is standard in problems of asymmetric information,  $M_i$  sets in state H the full-information best response to  $q_{Hj}$ , a feature known as "no distortion at the top". In state L,  $M_i$  sets the full-information best response only if p = 0. Otherwise,  $M_i$  offers a quantity below the full-information best response, in order to reduce the retailer's incentive to mimic L in state H, which enables the manufacturer to reduce the retailer's information rents.

To summarize the static benchmark, the equilibrium quantities are  $q_H^S$  and  $q_L^S$  and each manufacturer earns the expected profit  $\Pi_M^S \equiv \Pi_M^S(q_H^S, q_L^S, q_H^S, q_L^S)$  while each retailer earns:

$$\Pi_R^S \equiv p \left( \pi_{Li}(q_L^S, q_L^S) - T_L^S \right) + (1 - p) \left( \pi_{Hi}(q_H^S, q_H^S) - T_H^S \right) = p \left[ \pi_H(q_L^S, q_H^S) - \pi_L(q_L^S, q_L^S) \right].$$

# 3 Repeated game and collusion

Suppose that the four firms play an infinitely repeated game. The static equilibrium in the previous section is an equilibrium in the dynamic game as well. It is supported by the firms' beliefs that in every period manufacturers offer the static contract regardless of the past behavior. Yet, a repeated game also supports collusive equilibria that are based on informal understandings between firms. Because collusion in this paper requires the collaboration of both the upstream manufacturers and the downstream retailers, it is possible to distinguish between two special cases of collusive outcomes:

<sup>&</sup>lt;sup>7</sup>The proof of Proposition 2 below shows that  $q_L^S$  is decreasing with p. Hence, I assume that p is not too high as to induce  $q_{Li}^S(q_{Lj},q_{Hj})=0$ .

- 1. Collusion on the monopoly profits In every period, each manufacturer offers its retailer a menu with the monopoly quantities, i.e., the quantities that maximize joint industry profits of all four firms. Note that the monopoly quantities are not necessarily the optimal quantities for the two manufacturers. This is because under asymmetric information, each manufacturer has to leave some of the total profit to its retailer as "information rents". Likewise, the monopoly quantities may not be the optimal goal of collusion for the two retailers.
- 2. Collusion on maximizing upstream profits Manufacturers coordinate on the quantities that maximize their own joint profits. These quantities take into account the manufacturers' incentive to coordinate on reducing the retailers' information rents.

The collusive mechanism is identical in the two collusive possibilities, as they only differ in the collusive quantities. Therefore, in this section I define the general collusive mechanism, and then the next sections study how this mechanism can support each of the collusive cases. Moreover, for each of the collusive possibilities, I compare the case where retailers take part of the collusive scheme and the case where retailers are excluded (on which I explain below).

Consider the following mechanism. In every period, the two manufacturers offer an identical dynamic menu,  $\{(q_H^D, T_H^D), (q_L^D, T_L^D)\}$  that does not necessarily satisfy the static individual rationality and incentive compatibility constraints from the previous section.<sup>8</sup> Then, retailers accept the menu and reveal the state by choosing a contract that corresponds to the "right" state of demand. All firms expect that as long as they play this dynamic equilibrium, firms will continue playing it in all future periods. Any observable deviation triggers the static equilibrium in all future periods.

Any dynamic menu,  $\{(q_H^D, T_H^D), (q_L^D, T_L^D)\}$ , has to satisfy the following three constraints. The first constraint,  $IC_M^D$ , is the manufacturers' incentive compatibility constraint. As is standard in the literature on tacit collusion, each  $M_i$  can offer the dynamic menu at the beginning of each period or deviate to another incentive compatible menu. Since any deviation is observable by  $M_j - R_j$  at the end of the period and triggers the static menu in all future periods,  $M_i$ 's optimal deviation is to its static, asymmetric-information best-responses given that  $R_j$  sells in the current period  $q_L^D$  ( $q_H^D$ ) in state L (H):  $q_{Li}^S(q_H^D, q_L^D)$  and  $q_{Hi}^S(q_H^D)$  as given by equation (4). In the current period,  $M_i$  earns from this deviation the expected profit given

<sup>&</sup>lt;sup>8</sup>I focus on stationary mechanisms because it is a repeated game with i.i.d states.

by (3), after plugging the best responses. Then, in all future periods,  $M_i$  earns the static asymmetric profit,  $\Pi_M^S$ . Hence:

$$IC_{M}^{D}: \quad \frac{pT_{H}^{D} + (1-p)T_{L}^{D}}{1-\delta} \ge \Pi_{Mi}^{S}(q_{Hi}^{S}(q_{H}^{D}), q_{Li}^{S}(q_{H}^{D}, q_{L}^{D}), q_{H}^{D}, q_{L}^{D}) + \frac{\delta}{1-\delta}\Pi_{M}^{S}. \tag{5}$$

The left-hand side (5) is  $M_i$ 's sum of discounted profits from maintaining collusion and the right-hand side is  $M_i$ 's one-period profit from deviating, followed by the sum of discounted profits from the competitive equilibrium.

Next, consider the constraints on the retailers. In the context of this model, when the competing manufacturer sell through privately informed and potentially forward-looking retailers, manufacturers can include the retailers in the collusive scheme in which case collusion is also "vertical". To see how, suppose that the retailers, too, can support or stop the collusive scheme if they deviate from the equilibrium in a certain period. In this case, the retailers' individual rationality and incentive compatibility constraints become dynamic. The first constraint,  $IR_L^D$ , is  $R_i$ 's dynamic individual rationality constraint in state L. It ensures that  $R_i$  prefers accepting the contract  $(q_L^D, T_L^D)$  in state L given that doing so maintains the equilibrium, over rejecting the contract and receiving the static menu (and the static expected information rents) in all future periods:

$$IR_{L}^{D}: \quad \pi_{L}(q_{L}^{D}, q_{L}^{D}) - T_{L}^{D} + \frac{\delta}{1 - \delta} \left[ p(\pi_{H}(q_{H}^{D}, q_{H}^{D}) - T_{H}^{D}) + (1 - p)(\pi_{L}(q_{L}^{D}, q_{L}^{D}) - T_{L}^{D}) \right] \geq (6)$$

$$0 + \frac{\delta}{1 - \delta} \left[ p(\pi_{H}(q_{L}^{S}, q_{H}^{S}) - \pi_{L}(q_{L}^{S}, q_{L}^{S})) \right].$$

Notice that this condition is derived for  $R_i$  given that  $M_j$  offers to  $R_j$  the dynamic menu and  $R_j$  accepts the contract that corresponds to state L,  $(q_L^D, T_L^D)$ . Moreover, if  $R_i$  deviates by not accepting the contract in state L,  $M_j - R_j$  observe it at the end of the period and in all future periods all firms play the static equilibrium.

The second constraint,  $IC_H^D$ , is the retailer's dynamic incentive compatibility constraint in state H. It ensures that  $R_i$  prefers accepting the contract  $(q_H^D, T_H^D)$  in state H given that doing so maintains the dynamic equilibrium, over accepting the contract  $(q_L^D, T_L^D)$ . In the latter case both manufacturers and  $R_j$  detect the deviation at the end of the period and then play the static menu in all future periods:

$$IC_{H}^{D}: \quad \pi_{H}(q_{H}^{D}, q_{H}^{D}) - T_{H}^{D} + \frac{\delta}{1 - \delta} \left[ p(\pi_{H}(q_{H}^{D}, q_{H}^{D}) - T_{H}^{D}) + (1 - p)(\pi_{L}(q_{L}^{D}, q_{L}^{D}) - T_{L}^{D}) \right] \geq (7)$$

$$\pi_{H}(q_{L}^{D}, q_{H}^{D}) - T_{L} + \frac{\delta}{1 - \delta} \left[ p((\pi_{H}(q_{L}^{S}, q_{H}^{S}) - \pi_{L}(q_{L}^{S}, q_{L}^{S})) \right].$$

To summarize, any menu satisfying conditions (5), (6) and (7) can be a dynamic collusive equilibrium that involves all four firms. At the first stage of every period, each  $M_i$  prefers offering  $\{(q_H^D, T_H^D), (q_L^D, T_L^D)\}$  over deviating to its best responses. At the second stage of every period, each  $R_i$  accepts the contract that corresponds to the true state.

Notice that the  $IR_L^D$  and  $IC_H^D$  constraints are relevant only when retailers are forward-looking and when manufacturers stop colluding following any observable deviation by one of the retailers. In this case, retailers take an active role in maintaining or breaking the collusive scheme. When the two retailers are myopic, or when the two manufacturers ignore any retailer's deviation and continue to offer the dynamic menu following a retailer's deviation, the collusive menu has to satisfy only the manufacturers' dynamic constraint,  $IC_M^D$  and the retailer's two static constraints,  $IR_L^S$  and  $IC_H^S$ , as given by (1) and (2), respectively. An equivalent scenario is when  $M_i$  deals with a different retailer in every period. In such cases, retailers do not take an active role in the collusive scheme and behave as if the game is static. This raises the question of what are the market conditions under which including retailers in the collusive scheme (i.e., breaking collusion following a retailer's deviation) facilitates or hinders collusion.

# 4 Collusion on the monopoly profits

The main question of this section is whether including the two retailers in the collusive scheme (through their dynamic constraints) facilitates or hinders collusion on the monopoly quantities. To this end, I compare the critical value of  $\delta$  that enables collusion given  $IR_L^D$  and  $IC_H^D$  with the critical value of  $\delta$  that enables collusion given  $IR_L^S$  and  $IC_H^S$ . The main conclusion of this section is that retailers have a positive (negative) contribution to the stability of collusion when the probability of a high demand is above (below) some threshold.

Suppose first that collusion is also "vertical", i.e., involves the two retailers. In order to solve for the highest possible value of  $\delta$  that supports the collusive equilibrium,  $IR_L^D$ ,  $IC_H^D$ 

and  $IC_M^D$  must hold in equality. I start by deriving  $M_i$ 's expected one-period profit given arbitrary  $q_{Li}$ ,  $q_{Hi}$ ,  $q_{Lj}$  and  $q_{Hj}$ , when  $R_i$  takes part in the collusive scheme. Solving  $IR_L^D$  and  $IC_H^D$  from (6) and (7) in equality for  $T_H^D$  and  $T_L^D$ , substituting into  $M_i$ 's expected one-period profits,  $pT_H^D + (1-p)T_L^D$ , yields:

$$\Pi_{Mi}^{D}(q_{Li}, q_{Hi}, q_{Lj}, q_{Hj}) = p\pi_{Hi}(q_{Hi}, q_{Hj}) + (1 - p)\pi_{Li}(q_{Li}, q_{Lj}) - p\left[\pi_{Hi}(q_{Li}, q_{Hj}) - \pi_{Li}(q_{Li}, q_{Lj})\right]$$

+ 
$$\left[\frac{\delta p(1+p)}{1+\delta p}\right] \left(\pi_{Hi}(q_{Li}, q_{Hj}) - \pi_{Li}(q_{Li}, q_{Lj}) - \left(\pi_{Hi}(q_L^S, q_H^S) - \pi_{Li}(q_L^S, q_L^S)\right)\right).$$
 (8)

When firms collude on the monopoly quantities,  $q_{Li} = q_{Lj} = q_L^M$ ,  $q_{Hi} = q_{Hj} = q_H^M$  and  $M_i$  and  $R_i$  earn in each period the expected profits:

$$\Pi_{Mi}^{D,M} \equiv \Pi_{Mi}^{D}(q_{L}^{M}, q_{H}^{M}, q_{L}^{M}, q_{H}^{M}),$$

$$\Pi_{Ri}^{D,M} = p\pi_{Hi}(q_H^M, q_H^M) + (1-p)\pi_{Li}(q_L^M, q_L^M) - \Pi_{Mi}^{D,M}.$$

As in the static, asymmetric information case,  $M_i$ 's profit as defined by (8) is the expected joint profits of  $M_i$  and  $R_i$  minus  $R_i$ 's information rents, evaluated at the monopoly quantities. In the dynamic case, when retailers take part in the collusive scheme,  $R_i$ 's information rents has two components. The last term of the first line in (8) is the "static" information rents. The second line is the additional profits that  $M_i$  can collect from  $R_i$  due to the dynamic  $IR_L^D$  and  $IC_H^D$ . This is the "dynamic" component of the retailer's information rents. If retailers are myopic or if the two manufacturers exclude the retailers from the collusive scheme (by setting  $T_H$  and  $T_L$  according to the static  $IR_L^S$  and  $IC_H^S$ ), the second line in (8) vanishes. Hence, manufacturers benefit from including retailers in the collusive scheme when  $\pi_{Hi}(q_L^M, q_H^M) - \pi_{Li}(q_L^M, q_L^M) > \pi_{Hi}(q_L^S, q_H^S) - \pi_{Li}(q_L^S, q_L^S)$ . The following proposition provides the initial intuition for this result (all proofs are in the Appendix):

Proposition 1. (retailers may benefit or hurt from collusion on the monopoly outcome) If  $\pi_{Hi}(q_L^M, q_H^M) - \pi_{Li}(q_L^M, q_L^M) > (<)\pi_{Hi}(q_L^S, q_H^S) - \pi_{Li}(q_L^S, q_L^S)$ :

- (i) retailers gain higher (lower) one-period information rents in the collusive equilibrium on the monopoly outcome than in the static equilibrium, for all  $\delta$ ;
- (ii) retailers' one-period information rents under collusion on the monopoly outcome are decreasing (increasing) with  $\delta$ .

Proposition 1 shows that retailers prefer the collusive equilibrium on the monopoly outcome over the static outcome if the static component of their information rents,  $\pi_{Hi}(q_L, q_H) - \pi_{Li}(q_L, q_L)$ , is higher given the monopoly quantities than given the static quantities. Yet, in such a case, including retailers in the collusive scheme by adopting their dynamic constraints reduces their information rents and in turn increases the manufacturer's profits. The following corollary summarizes this result.

Corollary 1. (When is it profitable for manufacturers to include their retailers in the collusive scheme on the monopoly outcome?) Including the retailers in the collusive scheme on the monopoly outcome increases the manufacturers' profits and facilitates collusion if and only if  $\pi_{Hi}(q_L^M, q_H^M) - \pi_{Li}(q_L^M, q_L^M) > \pi_{Hi}(q_L^S, q_H^S) - \pi_{Li}(q_L^S, q_L^S)$ .

The intuition for this result is the following. When retailers' information rents given the monopoly quantities are higher than given the static quantities, reverting back to the static equilibrium serves as a punishment not only for the two manufacturers – as in standard "horizontal" collusion – but also for the two retailers. In such a case, forward - looking retailers have an incentive to maintain the collusive equilibrium. This in turn makes such collusion more feasible when retailers are included, i.e., when collusion involves  $IR_L^D$  and  $IC_H^D$  rather than  $IR_L^S$  and  $IC_H^S$ .

The results above raise the question of whether  $\pi_{Hi}(q_L^M, q_H^M) - \pi_{Li}(q_L^M, q_L^M)$  is higher or lower than  $\pi_{Hi}(q_L^S, q_H^S) - \pi_{Li}(q_L^S, q_L^S)$ . To this end, it is useful to compare between the competitive and the monopoly quantities. While the literature on collusion mainly focused on restricting output, i.e., collusion on quantities below the competitive quantities, in this model collusion may take a different form. Because of asymmetric information between retailers and their manufacturers, collusion on the monopoly quantities may involve collusion on a higher quantity than the competitive one. The following proposition compares between the monopoly and the competitive quantities.

### Proposition 2. (Comparison between the competitive and monopoly quantities)

- (i) For low values of p, the monopoly quantities in both states are below the competitive quantities. That is,  $q_L^S > q_L^M$  if p is sufficiently low. Moreover, for all  $p \in [0,1]$ ,  $q_H^S > q_H^M$ ;
- (ii)  $q_L^S$  is decreasing in p.

(iii) The monopoly quantity in state L can be higher then the competitive quantity if p is sufficiently high. That is, when  $\partial \pi_{Hi}(q_L^M, q_H^M)/\partial q_i > \partial \pi_{Li}(q_L^M, q_L^M)/\partial q_i$ , there is a threshold in p such that  $q_L^S < q_L^M$  if p is sufficiently high.

To illustrate the last part of Proposition 2, consider the following example:

**Example.** (Homogeneous products and linear demand) Suppose that the two supply chains sell homogeneous products. There are no production or retail costs and the inverse demand functions are  $p_H(q_i, q_j) = v_H - q_i - q_j$  and  $p_L(q_i, q_j) = v_L - q_i - q_j$ , where  $v_H > v_L > pv_H$ .  $q_i = v_H + q_i + q_$ 

$$q_H^S = \frac{v_H}{3}, \quad q_L^S = \frac{3v_L - 2pv_H}{9 - 6p} \quad and \quad q_H^M = \frac{v_H}{4}, \quad q_L^M = \frac{v_L}{4}.$$

Hence,  $q_H^S > q_H^M$  for all p,  $v_H$  and  $v_L$ . Yet,  $q_L^S < q_L^M$  if and only if:  $v_H > \frac{6}{5}v_L$  and  $\frac{3v_L}{8v_H - 6v_L} .$ 

In comparison with the monopoly outcome, the static, competitive outcome on one hand increases quantities because of the standard competitive effect. Yet, asymmetric information has the opposite effect of deriving manufacturers to distort the quantity in state L downward, in order to reduce the retailers' information rents. Because this second effect only holds in state L, only the first effect holds in state H and consequently the quantity under competition is higher than the monopoly quantity. Yet, in state L the second effect dominates when state H is likely (p is high) and the demand in state H is sufficiently large ( $v_H$  is high enough), because then manufacturers have a strong incentive to reduce the information rents in state H by distorting their quantities in state L downward.

These results are important for explaining how dynamics enable firms to collude on the monopoly outcome. Recall that the retailer's information rents depend on the retailers' incentive to report the true state, which in turn depend on  $q_L$ . This is because when a retailer miss-represent state H as state L, the retailer is "punished" by selling  $q_L$  instead of  $q_H$ . When p is small such that  $q_L^S$  is high relative to  $q_L^M$ , retailers face a stronger punishment and consequently a lower information rents under the monopoly quantities than under the static quantities. In this case, retailers do not have an incentive to facilitate collusion on the monopoly outcome. Yet, when p is high such that  $q_L^M$  is high relative to  $q_L^S$ , retailers

<sup>&</sup>lt;sup>9</sup>The condition  $v_L > pv_H$  ensures that  $q_L^S > 0$ .

benefit from higher information rents under collusion on the monopoly quantities than under competition, hence retailers facilitate such collusion.

Let  $\delta^{M,D}$  denote the threshold of  $\delta$  above which collusion on the monopoly outcome is an equilibrium, given that retailers are included in the collusive scheme. This threshold solves the constraints  $IR_L^D$ ,  $IC_H^D$  and  $IC_M^D$  in equality, evaluated at the monopoly quantities. Likewise, let  $\delta^{M,S}$  denote the threshold of  $\delta$  above which collusion on the monopoly outcome is an equilibrium, given the retailers' static constraints. That is, the solution to  $IR_L^S$ ,  $IC_H^S$  and  $IC_M^D$  in equality, evaluated at the monopoly quantities. Including retailers in the collusive scheme facilitates collusion when  $\delta^{M,D} < \delta^{M,S}$ . The comparison between  $\delta^{M,D}$  and  $\delta^{M,S}$  depends only on the manufacturer's collusive profits in the two collusive schemes. This is because the quantities are identical in the two schemes, implying that the manufacturer's profit from deviation are also the same. The following corollary is a direct consequence of the analysis so far:

Corollary 2. (Forward-looking retailers hinder collusion on the monopoly outcome when a low demand is more likely) If p is sufficiently small, including retailers in the collusive scheme hinders collusion on the monopoly outcome:  $\delta^{M,D} > \delta^{M,S}$ . Yet when p is sufficiently high and  $\pi_{Hi}(q_L^M, q_H^M) - \pi_{Li}(q_L^M, q_L^M) > \pi_{Hi}(q_L^S, q_H^S) - \pi_{Li}(q_L^S, q_L^S)$ , retailers facilitate collusion on the monopoly outcome:  $\delta^{M,D} < \delta^{M,S}$ .

To illustrate the second part of the corollary and to show when does  $\delta^{M,D} < \delta^{M,S}$ , consider the linear demand example. Then, there is a threshold:

$$\widehat{p} = \frac{16v_H - 3v_L}{2(16v_H - 9v_L)} - \frac{2}{16v_H - 9v_L} \sqrt{16v_H^2 - 21v_H v_L + 9v_L^2},\tag{9}$$

such that for  $p < \widehat{p}$   $(p > \widehat{p})$ ,  $\pi_{Hi}(q_L^M, q_H^M) - \pi_{Li}(q_L^M, q_L^M) < (>)\pi_{Hi}(q_L^S, q_H^S) - \pi_{Li}(q_L^S, q_L^S)$  and consequently  $\delta^{M,D} > (<)\delta^{M,S}$ . Figure 1 illustrates this result. For  $p > \widehat{p}$ , it is easier to maintain the collusion on the monopoly outcome with forward-looking retailers than with myopic retailers, because retailers gain higher information rents with the monopoly quantities than with the static quantities. Notice that in this case for high p (above  $\widetilde{p}$ ), it is impossible to maintain the monopoly outcome without forward-looking retailers for all values of  $\delta$ , because the retailers' incentive to deviate from truthful telling is too high. The opposite case occurs when  $p < \widehat{p}$ , where it is easier to maintain the monopoly outcome without including the retailers. Notice also that for p = 0,  $\delta^{M,D} = \delta^{M,S}$ , because manufacturers do not pay

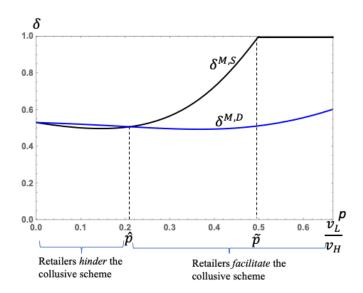


Figure 1:  $\delta^{M,D}$  and  $\delta^{M,S}$  as a function of p (given the linear demand example, when  $v_H = 3$  and  $v_L = 2$ )

retailers information rents, hence retailers do not play a positive or negative role in the collusive scheme.

# 5 Collusion on upstream profits

When retailers have private information, manufacturers do not earn all the collusive profit because they need to leave retailers with information rents. Hence, collusion on the quantities that maximizes total industry profits may not be the optimal strategy for manufacturers. In this section I consider collusion on the quantities that maximize the manufacturer's joint profit, i.e., upstream profits. I ask three questions. First, what are the features of these quantities and how they are affected by the repeated interactions between manufacturers and their retailers. Second, when is it easier to maintain collusion on upstream profits, in comparison with maintaining collusion on monopoly profits. Third, whether including retailers in the collusive scheme on upstream profits facilitates collusion. The main conclusions of this section are that manufacturers find it optimal to coordinate on a quantity above (below) the monopoly quantity when demand is high (low). In comparison with collusion on the monopoly profits, collusion on upstream profits is easier to maintain when the probability of a high demand is sufficiently high. Finally, forward-looking retailers facilitate upstream

collusion when the probability of high demand is high.

Consider a dynamic equilibrium where in each period the two manufacturers offer the quantities that maximize their joint profit given that  $IR_L^D$  and  $IC_H^D$  hold in equality and retailers accept. As before, any observable deviation at an end of a period (either a manufacturer deviates from the quantities that maximize upstream profits, or a retailer deviates by rejecting a contract or misrepresenting the state) is followed by a diversion to the static equilibrium.

Let  $q_H^U$  and  $q_L^U$  denote the quantities that maximize joint upstream profits,

$$\Pi_M^D(q_L, q_H) \equiv \Pi_{Mi}^D(q_L, q_H, q_L, q_H) + \Pi_{Mi}^D(q_L, q_H, q_L, q_H).$$

Using the definition of  $\Pi_{Mi}^D(q_{Li}, q_{Hi}, q_{Lj}, q_{Hj})$  from (8), the first order conditions of  $q_H^U$  and  $q_L^U$ , respectively, are:

$$\frac{\partial \Pi_M^D(q_L, q_H)}{\partial q_H} = \frac{\partial \pi_{Hi}(q_H^U, q_H^U)}{\partial q_i} + \frac{\partial \pi_{Hj}(q_H^U, q_H^U)}{\partial q_i} - \left[\frac{1-\delta}{1+\delta p}\right] \frac{\partial \pi_{Hj}(q_L^U, q_H^U)}{\partial q_i} = 0, \tag{10}$$

$$\frac{\partial \Pi_M^D(q_L, q_H)}{\partial q_L} = \frac{\partial \pi_{Li}(q_L^U, q_L^U)}{\partial q_i} + \frac{\partial \pi_{Lj}(q_L^U, q_L^U)}{\partial q_i} - \left[ \frac{(1 - \delta)p}{1 - \delta p^2} \right] \frac{\partial \pi_{Hi}(q_L^U, q_H^U)}{\partial q_i} = 0. \tag{11}$$

The first two terms in (10) are the first-order condition of the monopoly profits with respect to  $q_H$  (and equal to zero at  $q_H^U = q_H^M$ ). The last term in (10) is the effect of the quantity set by  $M_i$  in state H on the information rents that  $M_j$  has to pay  $R_j$ . Hence, under upstream collusion, the two manufacturers' joint interest is not only to coordinate on the monopoly quantities, but also on reducing each other's information rents. Likewise, the first two terms in (11) are the first-order condition of the monopoly profits with respect to  $q_L$  (and equal to zero at  $q_L^U = q_L^M$ ), while the last term is the effect of the quantity set by  $M_i$  in state L on  $R_i$ 's information rents. The following proposition characterizes the features of  $q_H^U$  and  $q_L^U$ :

Proposition 3. (Collusion on upstream profits involves upward (downward) distortion in state H(L)) The quantities that maximize the manufacturers' joint profits involve a quantity above (below) the monopoly quantity in state H(L):  $q_H^U > q_H^M$  and  $q_L^U < q_L^M$ . Moreover,  $q_H^U(q_L^U)$  is decreasing (increasing) in  $\delta$  and converges to the monopoly quantities as  $\delta \to 1$ .

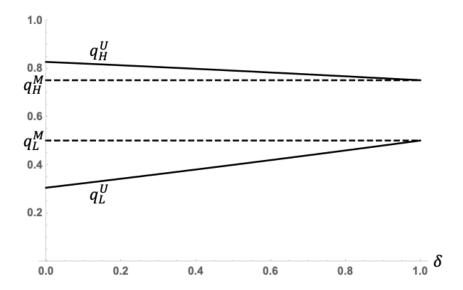


Figure 2: The upstream collusive quantities,  $q_H^U$  and  $q_L^U$ , as a function of  $\delta$  (given the linear demand example when  $v_H=3$ ,  $v_L=2$  and  $p=\frac{1}{2}$ )

Figure 2 illustrates the results of Proposition 3. The proposition finds two main results with implications to the comparison between collusion on upstream profits and on monopoly profits. The first main result is that in state H, manufacturers coordinate on a quantity above the monopoly quantity. This result differs from the standard result of "no distortion at that top" in the literature on asymmetric information. The intuition is that  $M_i$  can reduce the information rents that  $M_j$  pays  $R_j$  by distorting  $q_{Hi}$  upward. This is because when the state is H and  $R_j$  reports that the state is L,  $R_j$  is "punished" by  $R_i$  through the high  $q_{Hi}$  that  $M_i$  supplies  $R_i$ . Hence, to maximize upstream profits, each manufacturer sets a high quantity in state H in order to reduce the information rents that its competitor is paying it's retailer. As for the quantity in state L, collusion on upstream profits involve the standard downward distortion due to each manufacturer's incentive to decrease its retailer's information rents. The second main result is that as retailers become forward-looking ( $\delta$ increases), manufacturers decrease (increase) the quantities in state H(L). Intuitively, when collusion is "vertical" and involves the two retailers, manufacturers can take advantage of the dynamic  $IR_L^D$  and  $IC_H^D$  to reduce the retailers' information rents. This is because when retailers gain a higher information rents under collusion than under the static game, retailers have an incentive to facilitate collusion. This, in turn, allows the two manufacturers to reduce the quantity distortion as retailers become more forward-looking and quantities converge to

their monopoly levels.

Remark: I assume that the gap between  $q_H^U$  and  $q_L^U$  is sufficiently small such that the  $\pi_{Hi}(q_L^U,q_H^U)-\pi_{Li}(q_L^U,q_L^U)>0$ . This assumption ensures that if  $\delta$  is close to 0, the gap between  $q_H^U$  and  $q_L^U$  is such that  $R_i$ 's static information rents in staten H is positive. Otherwise, The quantities that maximize upstream profits has a corner solution in which both  $IR_L^D$  and  $IR_H^D$  bind. In the linear demand example, it is possible to show that  $\pi_{Hi}(q_L^U,q_H^U)-\pi_{Li}(q_L^U,q_L^U)>0$  and consequently there is an internal solution to  $q_H^U$  and  $q_L^U$  for all  $\delta$  when 0 .

Next, I turn to the question of whether upstream collusion is easier to maintain than collusion on the monopoly outcome. I compare the two collusive schemes given that they both include the retailers (i.e.,  $IR_L^D$  and  $IC_H^D$  are dynamic). Let  $\delta^{U,D}$  denote the lowest possible  $\delta$  that maintains collusion on upstream profits given dynamic retailers. This  $\delta^{U,D}$  solves the constraints  $IR_L^D$ ,  $IC_H^D$  and  $IC_M^D$  in equality, evaluated at  $q_L^U$  and  $q_H^U$ . Recall that  $\delta^{M,D}$  is the lowest possible  $\delta$  that maintains collusion on the monopoly outcome, given dynamic retailers. The comparison between  $\delta^{U,D}$  and  $\delta^{M,D}$  depends on the model's parameters. Applying the linear demand example yields a complex polynomial solution to  $\delta^{U,D}$ . Using numerical simulations I obtain the following results:

# Result 1. (Collusion on upstream profits is easier to maintain than on monopoly profits when p is high and $v_L$ is small) Consider the linear demand example:

- (i) When  $v_L$  is small in comparison with  $v_H$ , collusion on the monopoly outcome is easier to maintain than collusion on upstream profits (i.e.,  $\delta^{U,D} > \delta^{M,D}$ ) when p is low, while for  $\delta^{U,D} < \delta^{M,D}$  otherwise;
- (ii) When  $v_L$  is high in comparison with  $v_H$ ,  $\delta^{U,D} > \delta^{M,D}$  for all values of p.

Figure 3 illustrates theses results. Panel (a) illustrates the case where  $v_L$  is small such that collusion on monopoly profits is easier to maintain then collusion on upstream profits (i.e.,  $\delta^{U,D} > \delta^{M,D}$ ) as long as p is not too high. Panel (b) illustrates the case where  $v_L$  is high such that  $\delta^{U,D} > \delta^{M,D}$  for all 0 .

The intuition for this result is that the comparison between  $\delta^{U,D}$  and  $\delta^{M,D}$  exhibits the following tradeoff. First, manufacturers' profits from colluding on upstream profits are higher

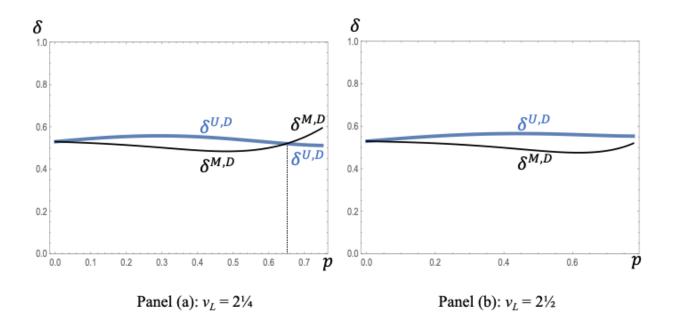


Figure 3:  $\delta^{U,D}$  and  $\delta^{M,D}$  as a function of p (given the linear demand example, when  $v_H = 3$ )

than colluding on the monopoly profits, as the latter profits do not maximize the manufacturers' joint profits. This effect makes collusion on upstream profits easier to maintain than collusion on monopoly profits. Second, each manufacturer's profit from deviating from collusion might also be higher when manufacturers collude on upstream profits. This second effect is stronger when the probability of state L is high. Recall that the quantity that maximizes upstream profits in state H (L) is higher (lower) than the monopoly quantity. Hence, the incentive to deviate from collusion is higher in state L than in state H, because then the manufacturer would like to deviate to a higher quantity. When  $v_L$  is small, the second effect dominates for a low p, while when  $v_L$  is high, the second effect dominates for all p.

Next, I turn to evaluate the effect of including forward-looking retailers in the collusive scheme on upstream profits. Manufacturers can collude on upstream profits without including the retailers, by dealing with myopic retailers or by ignoring a retailer's deviation from the collusive scheme. This raises the question of whether retailers facilitate of hinder collusion on upstream profit.

Let  $q_L^{U,S}$  and  $q_H^{U,S}$  denote the quantities that maximize joint manufacturers' profits when retailers are static. The  $q_L^{U,S}$  and  $q_H^{U,S}$  are the solutions to the first-order-conditions (11) and

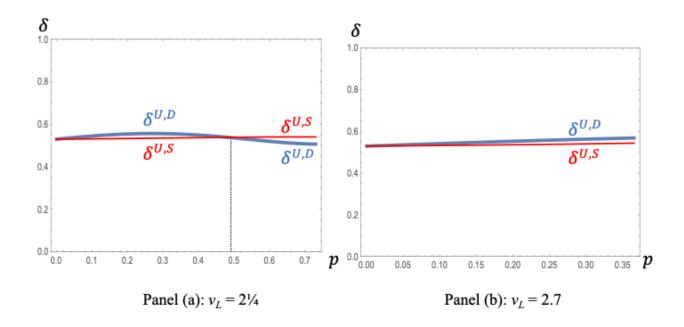


Figure 4:  $\delta^{U,D}$  and  $\delta^{M,D}$  as a function of p (given the linear demand example, when  $v_H = 3$ )

(10), evaluated at  $\delta=0$ . Because  $q_L^U$  is increasing with  $\delta$  while  $q_H^U$  is decreasing with  $\delta$ ,  $q_L^{U,S}$  and  $q_H^{U,S}$  are at their lowest and highest levels of  $q_L^U$  and  $q_H^U$ , respectively (as shown at Figure 2 when  $\delta=0$ ). Let  $\delta^{U,S}$  denotes the lowest value of  $\delta$  that sustains collusion on upstream profits when retailers are myopic. This  $\delta^{U,S}$  solves  $IR_L^S$ ,  $IC_H^S$  and  $IC_M^D$  in equality, evaluated at  $q_L^{U,S}$  and  $q_H^{U,S}$ . For tractability, I compare  $\delta^{U,S}$  with  $\delta^{U,D}$  using the linear demand example.

Figure 4 illustrates  $\delta^{U,D}$  and  $\delta^{U,S}$  as a function of  $\delta$ . Panel (a) illustrates the case where  $v_L$  is small, hence collusion with myopic retailers is easier to sustain then collusion with forward-looking retailers ( $\delta^{U,S} < \delta^{U,D}$ ) when p is below a threshold. In Panel (b),  $v_L$  is high and consequently  $\delta^{U,S} < \delta^{U,D}$  for all relevant values of p.

Following the same intuition as in Section 4, retailers' information rents in the static equilibrium can be higher or lower than under collusion on upstream profits. When p is small, then  $\delta^{U,D} > \delta^{U,S}$  because the gap between  $q_H^{U,D}$  and  $q_L^{U,D}$  is wide, hence a low level of information rents are needed to motivate retailers to reveal the state under upstream collusion. Yet, this reduces their incentive to facilitate the collusive scheme. The opposite case accuses when p is high.

# 6 Conclusion

This paper considers an infinitely repeated game between two vertical supply chains. Each retailer has private information concerning the demand, so manufacturers offer a menu of contracts and pay retailers information rents. The repeated interaction between the two supply chains enables firms to collude, and the repeated interaction within each supply chain enables the manufacturers to include their retailers in the collusive scheme. Studying such markets has implications for competition policy. While from a legal perspective, it is rather difficult to prosecute firms for engaging in tacit collusion, detecting such collusion enables competition authorities to evaluate the market power and concentration in such markets. Moreover, in real-life, such collusion may involve informal communication which can be illegal.

The paper finds that retailers facilitate collusion when their information rents in the collusive equilibrium are higher than in the competitive outcome. When firms collude on the monopoly outcome, retailers facilitate collusion when the probability of a high demand is high. Otherwise, manufacturers are better off without including their retailers in the collusive scheme, hence ignore a retailer's deviation from the collusive path. This result can explain why, in some recent legal cases, collusion involved both upstream and downstream firms, while other legal cases involved only the upstream firms. For policy, this result implies that when competition authorities detect collusion among upstream firms, it is also important to investigate the role of their retailers in facilitating such collusion. In particular, when the market demand fluctuates over time, such that information concerning the demand is important for writing the distribution contract, retailers could potentially participate in such collusion.

Because asymmetric information forces manufacturers to leave their retailers a share of the collusive profits, the paper finds that manufacturers can benefit from colluding on the quantities that maximize upstream profits, rather than total profits. In this case, collusion involves an upward (downward) deviation in periods of high (low) demand, in comparison with the monopoly quantities. The policy implication of this result is that in order to detect collusion, competition authorities should not look at the quantity of the current period alone, but on the stream of quantities along time, and try to identify cases in which low demand result in an ultra low quantity.

Finally, the paper finds that when the probability of a low demand is high enough, collu-

sion on monopoly profits is easier to maintain than collusion on upstream profits. Although the two manufacturers earn higher collusive profits when colluding on maximizing upstream profits, each manufacturer's incentive to deviate is also higher, which makes collusion more difficult to maintain than collusion on monopoly profits.

### **Appendix**

Below are the proofs of Propositions 1 - 3.

### **Proof of Proposition 1:**

Part (i):  $R_i$ 's information rents in the collusive equilibrium on the monopoly outcome are:

$$\Pi_{Ri}^{D,M} = p \left[ \pi_H(q_L^M, q_H^M) - \pi_L(q_L^M, q_L^M) \right]$$
(12)

$$-\left[\frac{\delta p(1+p)}{1+\delta p}\right] \left(\pi_{H}(q_{L}^{M},q_{H}^{M}) - \pi_{L}(q_{L}^{M},q_{L}^{M}) - \left(\pi_{H}(q_{L}^{S},q_{H}^{S}) - \pi_{L}(q_{L}^{S},q_{L}^{S})\right)\right).$$

Hence:

$$\Pi_{Ri}^{D,M} - \Pi_{Ri}^{S} = \frac{p(1-\delta)}{1+\delta p} \left[ \pi_H(q_L^M, q_H^M) - \pi_L(q_L^M, q_L^M) - (\pi_H(q_L^S, q_H^S) - \pi_L(q_L^S, q_L^S)) \right],$$

which is positive (negative) when the sign of the squared brackets is positive (negative). Part (ii): The term  $\left[\frac{\delta p(1+p)}{1+\delta p}\right]$  is increasing in  $\delta$ , implying that the retailers' information rents are decreasing in  $\delta$  when the term in the squared brackets is positive.

### **Proof of Proposition 2:**

I start by showing that  $q_{Hi}^S(q_H^M) > q_H^M$ , which implies that  $q_H^S > q_H^M$ . Recall that  $q_H^M$  is the solution to  $\partial \pi_{Hi}(q_H^M, q_H^M)/\partial q_i + \partial \pi_{Hj}(q_H^M, q_H^M)/\partial q_i = 0$ , where the second term is negative because  $\partial \pi_{\theta j}(q_{\theta j}, q_{\theta i})/\partial q_i < 0$ , implying that  $\partial \pi_{Hi}(q_H^M, q_H^M)/\partial q_i > 0$ . Recall further that  $q_{Hi}^S(q_H^M)$  is the solution to  $\partial \pi_{Hi}(q_{Hi}, q_H^M)/\partial q_i = 0$ . Because evaluated at  $q_{Hi}^S(q_H^M) = q_H^M$ ,  $\partial \pi_{Hi}(q_H^M, q_H^M)/\partial q_i > 0$ , I have that  $q_{Hi}^S(q_H^M) > q_H^M$ .

Next, consider the comparison between  $q_L^S$  and  $q_L^M$ . To show that  $q_{Li}^S(q_L^M, q_H^M) > q_L^M$  when p = 0, recall that  $q_{Li}^S(q_L^M, q_H^M)$  is the solution to:

$$\frac{\partial \pi_{Li}(q_L^M, q_L^M)}{\partial q_i} - p \frac{\partial \pi_{Hi}(q_L^M, q_H^M)}{\partial q_i} = 0.$$
 (13)

When p=0, the second term in (13) vanishes and  $q_{Li}^S(q_L^M, q_H^M) > q_L^M$  by applying the same argument as the first part of this proof for the case where  $\theta=L$ . When p>0,  $\partial \pi_{Hi}(q_L^M, q_H^M)/\partial q_i > \partial \pi_{Hi}(q_H^M, q_H^M)/\partial q_i > 0$ , where the first inequality follows because by assumption  $\pi_{Hi}(q_i, q_j)$  is concave in  $q_i$  (hence  $\partial \pi_{Hi}(q_i, q_j)/\partial q_i$  is decreasing in  $q_i$ ) and because  $q_H^M > q_L^M$ . The second inequality follows by the first pat of this proof. I therefore have that (13) is decreasing in p, implying that  $q_{Li}^S(q_L^M, q_H^M)$  and consequently  $q_L^S$  is decreasing in p.

Finally, it is possible that  $q_L^S < q_L^M$ , which holds for high values of p if and only if evaluated at p = 1, (13) is negative, or:  $\partial \pi_{Hi}(q_L^M, q_H^M)/\partial q_i > \partial \pi_{Li}(q_L^M, q_L^M)/\partial q_i$ .

### Proof of Proposition 3:

Consider first  $q_H^U$ . I show that the first-order-condition of  $q_H^U$ , (10), is positive when evaluated at  $q_H^U = q_H^M$  and  $q_L^U = q_L^M$ . The first two terms in (10) are the first-order-condition for the monopoly quantity hence equals 0 at  $q_H^U = q_H^M$  and  $q_L^U = q_L^M$ . The last term is positive for all quantities because by assumption  $\partial \pi_{Hj}(q_L^U, q_H^U)/\partial q_i < 0$ . Because the term  $\left[\frac{1-\delta}{1+\delta p}\right]$  is positive at  $\delta = 0$ , positive and decreasing with  $\delta$  for  $\delta > 0$  and equals 0 at  $\delta = 1$ , it follows that  $q_H^U > q_H^M$  for  $\delta = 0$ ,  $q_H^U$  is decreasing in  $\delta$  and converges to  $q_H^M$  as  $\delta \to 1$ .

Next consider  $q_L^U$ . I show that the first-order-condition of  $q_L^U$ , (11), is negative when evaluated at  $q_L^U = q_L^M$  and  $q_H^U = q_H^M$ . The first two terms in (11) are the first-order-condition for the monopoly quantity hence equals 0 at  $q_H^U = q_H^M$  and  $q_L^U = q_L^M$ . The last term, evaluated at  $q_H^U = q_H^M$  and  $q_L^U = q_L^M$  is negative when  $\partial \pi_{Hi}(q_L^M, q_H^M)/\partial q_i > 0$ . To see why  $\partial \pi_{Hi}(q_L^M, q_H^M)/\partial q_i > 0$ , recall that  $\partial \pi_{Hi}(q_H^M, q_H^M)/\partial q_i > 0$  and  $\partial^2 \pi_{Hi}(q_i, q_H^M)/\partial q_i^2 < 0$ . Because  $q_H^M > q_L^M$ ,  $\partial \pi_{Hi}(q_L^M, q_H^M)/\partial q_i > \partial \pi_{Hi}(q_H^M, q_H^M)/\partial q_i > 0$  and equals 0 at  $\delta = 1$ , it follows that that  $q_L^U < q_L^M$  for  $\delta < 1$ ,  $q_L^U$  is increasing in  $\delta$  and converges to  $q_L^M$  as  $\delta \to 1$ .

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